Suppressed Quenching and Strong-Coupling of Purcell-Enhanced Single-Molecule Emission in Plasmonic Nanocavities

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Supporting Information

ABSTRACT: An emitter in the vicinity of a metal nanostructure is quenched by its decay through nonradiative channels, leading to the belief in a zone of inactivity for emitters placed within <10 nm of a plasmonic nanostructure. Here we demonstrate and explain why in tightly coupled plasmonic resonators forming nanocavities “quenching is quenched” due to plasmon mixing. Unlike isolated nanoparticles, such plasmonic nanocavities show mode hybridization, which can massively enhance emitter excitation and decay via radiative channels, here experimentally confirmed by laterally dependent emitter placement through DNA-origami. We explain why this enhancement of excitation and radiative decay can be strong enough to facilitate single-molecule strong coupling, as evident in dynamic Rabi-oscillations.

KEYWORDS: nanoplasmonics, nanophotonics, light–matter strong coupling, fluorescence enhancement, quenching

The lifetime of an excited atomic state is determined by the properties of the atom and its environment, first theoretically suggested by Purcell1 and followed by experimental demonstration by Goy et al.2 Subsequent experiments further verified this by placing atomic emitters within various optical-field-enhancing geometries.3−5 Plasmonic structures have the ability to massively enhance electromagnetic fields and, therefore, dramatically alter the excitation rate of an emitter. However, it is well-known that placing an emitter close to an isolated plasmonic nanostructure (<10 nm) quenches its fluorescence.6−9 Analysis by Anger et al.6 showed this is due to the coupling of the emitter to nonradiative higher-order plasmonic modes that dissipate its energy. This “zone of inactivity” was previously believed to quench all quantum emitters.

However, recent advancements have shown that an emitter’s emission rate can be enhanced with plasmonic nanonanantennas.10−17 which efficiently convert far-field radiation into a localized field and vice versa. As first theoretically explained by Jun et al.,16 a single emitter placed into near-contact with a plasmonic nanoantenna can efficiently couple with the antenna’s plasmonic modes and overcome quenching.16,20 This was experimentally demonstrated by Hoang et al.17 who showed that a quantum dot in a 12 nm nanogap exhibits ultrafast spontaneous emission. What however remains unclear is if this enhanced emission is strong enough to allow for single emitter strong coupling with plasmons.

In this Article we demonstrate and explain why quenching is substantially suppressed in plasmonic nanocavities to such a degree that can indeed facilitate light–matter strong coupling of a single molecule at room temperature as we recently demonstrated experimentally.21,22 This is due to (i) the dramatic increase in the emitter excitation (similar to plasmonic antennas) and (ii) the changed nature of higher-order modes that acquire a radiative component and, therefore, increase the quantum yield of the system. Modes in plasmonic nanocavities are not a simple superposition of modes from isolated structures but, instead, are hybrid-plasmonic states.23−27 Hence, higher-order modes that are dark for an isolated spherical nanoparticle radiate efficiently for tightly coupled plasmonic structures,26,29 significantly reducing the nonradiative decay and quenching. By comparing an isolated nanoparticle (NP) with a nanoparticle-on-mirror (NPoM) nanocavity (equivalent alternatives being nanoparticle dimers with <3 nm gap), we quantify their different radiative and nonradiative channels, explaining the mechanism that leads to suppression of quenching in plasmonic nanocavities. We then experimentally confirm the suppression of quenching in plasmonic nanocavities, using DNA-origami to control the position of a single emitter in the nanogap. A full time-domain Maxwell-Bloch approach finally allows us to directly contrast through 3D Finite-Difference Time-Domain (FDTD) simulations, the (spatiotemporal) dynamics of single quantum emitters in both the NP and NPoM cases and in weak and strong coupling.

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**SUPPRESSED FLUORESCENCE QUENCHING**

The fluorescence rate $\gamma_{em}$ of an emitter generally depends on its excitation rate ($\gamma_{exc}$) and its radiative decay rate (i.e., quantum yield, $\eta = \gamma_{rad}/\gamma_{tot}$) as

$$\gamma_{em} = \gamma_{exc} \eta = \gamma_{exc} \left( \frac{\gamma_{rad}}{\gamma_{tot}} \right)$$  

(1)

where $\gamma_{rad}$ and $\gamma_{tot}$ are the emitter’s radiative and total (Purcell factor) decay rates. The normalized excitation rate is governed by the field enhancement at the position of the emitter, and assuming that the environment does not affect the emitter’s polarizability we have

$$\tilde{\gamma}_{exc} = \frac{\gamma_{exc}}{\gamma_{tot}} = \left| \frac{\hat{\mu} \cdot \mathbf{E}(r = 0)}{\hat{\mu} \cdot \mathbf{E}_0(r = 0)} \right|^2$$  

(2)

where $\hat{\mu}$ is the emitter’s polarizability unit vector, $\mathbf{E}(r = 0)$ is the total (incident and scattered) electric field and $\mathbf{E}_0(r = 0)$ is the incident field at $r = 0$, where the emitter is placed. Assuming that the nonradiative decays are due to the Ohmic losses of the metal alone, the quantum yield of an emitter with radiative decay rate $\gamma_{rad} = \gamma_{tot} - \gamma_{nr}$ is calculated via $\gamma_{nr} \propto \int \text{Re}\{j(r) \cdot \mathbf{E}_{em}^*(r)\} \cdot \mathbf{E}_0(r) \cdot dr$, where $j$ is the induced current density within the volume $V$ and $\mathbf{E}_{em}$ is the field emitted by the emitter.

In the case of an isolated spherical nanoparticle (or a plasmonic nanoantenna), an emitter couples dominantly to the nanoparticle dipolar (first-order) mode. However, as the emitter approaches the nanoparticle, it couples increasingly to higher-order modes, which are dark. This leads to its energy dissipation via Ohmic losses (quenching). Figure 1(a) shows the normalized fluorescence rate $\tilde{\gamma}_{em} = \eta \tilde{\gamma}_{exc}$ for an isolated NP, calculated for a classical dipole approaching the structure, using FDTD simulations. Quenching appears when the emitter is placed at $z < 10$ nm, in line with previously reported results. By contrast, similar calculations for the NPoM nanocavity with the emitter always in the center of the nanocavity (Figure 1b) reveal that the emission rate increases by several orders of magnitude (note the log-scale). As $z$ decreases, the gap between nanoparticle and mirror reduces, and both plasmonic surfaces approach the emitter, but $\tilde{\gamma}_{em}$ dramatically increases. Since the emission rate is a product of the excitation and radiative rates, we plot them separately (Figures 1c and S1) for both an isolated NP and the nanocavity. As the emitter is progressively confined within the nanocavity, its excitation rate dramatically increases, due to the very high confinement of the plasmon modes within the gap. Additionally, the quantum yield $\eta$ of the nanocavity outperforms the isolated NP by more than an order of magnitude as the gap decreases. While nonlocal effects can affect the quantitative rates of emission, excitation, and quantum yield of both structures at subnm spacings, no qualitative change is expected on their behavior (see Supporting Information S2 for more discussion).

To illuminate the origin of these different behaviors, we adapt the analytical description of coupled plasmon modes. Isolated spherical nanoparticles are well accounted for by Mie theory, but the problem of two coupled plasmonic nanoparticles is analytically more complex to determine. It has been solved in the quasi-static limit using several techniques, such as transformation optics and multipole expansion. How- ever, it is more appropriate to formulate the problem as the coupling of the bare plasmonic modes from the two structures. Adapting this description for the NPoM (by approximating the mirror as a large sphere of radius $r_m = 1 \mu m$), the field enhancement in the middle of the nanocavity gap is given by

$$\frac{E(r = 0)}{E_0} \approx \alpha^{NP} \left( \frac{R}{R + z} \right)^3 + \alpha^m \left[ 1 + \sum_{l=2}^{\infty} \frac{\omega_l \omega_{l'}}{\omega_l - \omega - i\gamma/2} \left( 1 + \frac{1}{2} \right)^2 \right]$$

where $R$ is the radius of the nanoparticle, $2z$ is the gap size assuming the emitter is in the middle of the gap, and $\omega_l$ is the resonant frequency of mode $l$, with $\omega_p$ and $\gamma$ the metal plasmon frequency and damping. The nanoparticle quasi-static polarizability $\alpha^{NP} = 2 \left( \frac{\omega_{em} - 1}{\omega_{em} + 1} \right)^3$, while the mirror polarizability $\alpha^m$ is given by Mie scattering (beyond the quasi-static limit) in ref 37. The first term provides the field enhancement contribution of the nanoparticle dipole mode, the first term in square brackets is the mirror dipole mode, and the second term in square brackets is the coupling of the mirror to the higher-order modes of the nanoparticle ($l \geq 2$). In Figure 1d, we plot this latter contribution of the coupling terms in eq 3 to the excitation rate (red lines) while truncating at increasingly higher-order modes. As the nanocavity gets smaller ($z < 10$ nm), the higher-order mode hybridization is needed to account for the dramatic increase of the NPoM excitation rate (seen in Figure 1c). Similarly, the quantum yield increases with increasingly higher-order hybridization between the two structures. Both these demonstrate that the mode hybridization of the coupled
plasmonic structures forming the nanocavity (Figure S2) alter the fluorescence rate of an emitter in a way that fully suppresses quenching.

The spectral dependence of the radiative, total, and excitation rates for both the isolated NP and the nanocavity, varying the nanoparticle diameter from 20 to 100 nm, show strongly contrasting behavior (Figure 2). Again, the emitter is 0.5 nm from the Au surfaces or at the center of the 1 nm gap. Isolated quasi-static nanoparticles (with 2R < 100 nm) possess diameter-independent modes (Figure 2a,c,e). However, the resonant wavelengths of the nanocavity modes are highly dependent on the system geometry28,38 (Figure 2b,d,f). The NPoM radiative decay rate \( \bar{\gamma}_{\text{rad}} = \gamma_{\text{rad}}/\gamma_0 \) normalized to the free space decay rate \( \gamma_0 \) is 3 orders of magnitude larger than for the isolated NP, with the NPoM dipole (l = 1) mode significantly red-shifting for larger nanoparticles. Additionally, the quadrupole NPoM mode (l = 2) strongly radiates and, for larger nanoparticles, has comparable radiative rates to the dipole (l = 1) mode, in great contrast with the isolated NP. These large \( \bar{\gamma}_{\text{rad}} \) suppress quenching and allow strong coupling dynamics to be radiated into the far-field.

The Purcell factor (normalized total decay rate \( \bar{\gamma}_{\text{tot}} = \gamma_{\text{tot}}/\gamma_0 \)) for both plasmonic structures shows a diameter-independent broad peak at \( \lambda_{pm} \approx 510 \) nm (Figure 2b,d,f), which corresponds to the superposition of multiple high-order plasmonic modes, recently referred to as a “pseudomode”.39 However, the negligible \( \bar{\gamma}_{\text{rad}} \) at \( \lambda_{pm} \) shows the large \( \bar{\gamma}_{\text{tot}} \) comes from emission coupled to the pseudomode decaying via nonradiative channels (\( \bar{\gamma}_{\text{tot}} = \bar{\gamma}_{\text{rad}} + \bar{\gamma}_{\text{fi}} \)). In contrast to recent proposals,3 this suggests the nanocavity pseudomode quenches emission almost entirely via nonradiative channels, as it does for isolated nanoparticles, suppressing any way to observe possible strong coupling dynamics. At the NPoM dipole and quadrupole resonant wavelengths, \( \bar{\gamma}_{\text{rad}} \sim \bar{\gamma}_{\text{tot}}/2 \), and therefore, information on the coherent energy exchange between the emitter and the plasmon modes is carried to the far-field and thus allows tracking of the hybrid states.

Additionally, the excitation rate \( \bar{\gamma}_{\text{exc}} \) of an emitter next to an isolated NP is 2 orders of magnitude smaller than for a 1 nm nanocavity (Figure 2e,f). Hence, for an isolated NP, where \( \bar{\gamma}_{\text{rad}} \ll \bar{\gamma}_{\text{tot}} \), an emitter is weakly excited and heavily quenched by higher-order modes. On the other hand, the NPoM nanocavity strongly excites the emitter with the dipole/quadrupole modes, with \( \bar{\gamma}_{\text{exc}} \) increasing for larger nanoparticles, but also significant energy is both radiated (\( \bar{\gamma}_{\text{rad}} \sim \bar{\gamma}_{\text{tot}}/2 \)) and exchanged between the emitter and plasmons. Due to the mode hybridization and radiative behavior of higher-order modes for the NPoM, its \( \bar{\gamma}_{\text{em}} \) is dramatically increased and, hence, allows the room-temperature strong coupling of a single emitter in plasmonic nanocavities to be experimentally measured.31

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**DNA-ORIGAMI CONTROLLED FLUORESCENCE MEASUREMENTS**

These findings are continued with experimental measurements, where we place a single Cy5 molecule within NPoM nanocavities formed by 80 nm diameter nanoparticles. DNA-origami40,41 is used to create a 5 nm thick spacer and to control the emitter position at nm lateral and vertical accuracies relative to the gold nanoparticle (Figures 3, inset, and S3). A two-layer DNA-origami plate (55 × 45 nm) is attached onto a gold substrate via thiol-modified staple strands. This is followed by hybridizing ssDNA-functionalized gold nanoparticles with complementary overhang staple strands onto the top of the origami.40 The position of the dye molecules with respect to the NP is varied by folding the origami with specific Cy5-modified staples at predefined positions from the center of the NP attachment groups. We illuminate the nanocavity with a high numerical aperture (NA 0.8) objective, filling the back focal plane of the aperture with 633 nm laser light. The emission rates are extracted from luminescence at 690 nm from >300 individual NPoM cavities. These intensities are normalized to a control dye molecule on a glass substrate. For more detail, see Supporting Information S4 and S5. Note that the sub-picosecond emission time scales here preclude any direct measurement of emission rates, for any position of the dye molecule, since current state-of-the-art equipment cannot resolve such fast decays.

The experimental emission rates at different lateral positions (Figure 3, black points) quantitatively match the numerically calculated emission rates for dipoles oriented along the z-axis and at 45°, as indicated. These results showing \( \bar{\gamma}_{\text{em}}(x,t) \) combine both positive and negative x, which are identical (Figure S4),

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**Figure 2.** Spectra for a vertically oriented emitter placed (a, c, e) 0.5 nm below an isolated NP and (b, d, f) inside a 1 nm wide NPoM nanocavity. (a, b) Normalized radiative decay rate \( \gamma_{\text{rad}} \), (c, d) normalized total decay rate \( \gamma_{\text{tot}} \) (Purcell factor), and (e, f) normalized excitation rate \( \gamma_{\text{exc}} \).

**Figure 3.** (a) Schematic diagram of the experimental setup where the Cy5 molecule is represented as a red arrow embedded within the DNA-origami, represented in blue. (b) Experimental (black) and numerical (red) emission intensities of a single Cy5 molecule inside a DNA-origami structure with 5 nm nanocavity gap and 80 nm diameter. The molecule, aligned at angle 0° and 45°, is laterally displaced by x from center of nanocavity and excited by a 633 nm laser.
placing the $x = 0$ particle center within an experimental error of ±2 nm. Different DNA-origami foldings result in slightly different dipole orientations, and partial melting of the double-stranded DNA together with slight imprecision in nanoparticle placement yield the uncertainty in emitter position. These small variations lead to different emission intensities in different NPoMs, shown as vertical error bars in the experimental data (Figure 3). It is, however, evident that an emitter in a plasmonic nanocavity does not quench, even if it is placed in the vicinity (<10 nm) of metal nanostructures, but instead its emission rate enhances.

**STRONG COUPLING DYNAMICS**

The dramatically enhanced $\gamma_{em}$ for NPoM is the reason that we can measure the strong coupling dynamics at room temperature. While the classical calculations presented so far provide useful insight into the radiative and nonradiative decay channels of these differing plasmonic systems, they cannot reveal the spatiotemporal dynamics of an emitter coupling to the plasmons. We thus now use a dynamic two-level Maxwell-Bloch description \(^\text{42}\) for the emitter, where the excited- ($N_2$) and ground-state ($N_1$) populations dynamics are described by

$$\frac{\partial^2 \mathbf{P}}{\partial t^2} + 2\Gamma \frac{\partial \mathbf{P}}{\partial t} + (\Gamma^2 + \omega_0^2) \mathbf{P} = -\frac{2\hbar}{\lambda} \mu^2 (N_2 - N_1) \mathbf{E}(t)$$

(3)

$$\frac{\partial N_2}{\partial t} = -\frac{\partial N_1}{\partial t} = -\gamma N_2 + \frac{1}{\hbar \omega_0} \left( \frac{\partial \mathbf{P}}{\partial t} + \Gamma \mathbf{P} \right) \mathbf{E}(t)$$

(4)

where $\mathbf{P}$ is the induced polarization, $\omega_0 = 2\pi/\lambda_0$ is the transition frequency, $\mu$ is the transition dipole moment, and $\gamma$ and $\Gamma$ are the relaxation and dephasing rates of the emitter. Here, we consider a realistic emitter with $\mu = 3.79 \mu_0$, $\gamma = 0.66 \mu eV$, and $\Gamma = 28 \text{ meV}$.\(^\text{21}\) The polarization response $\mathbf{P}$ is driven by the local E field from eqns 3 and 4 and injects photons that can couple back to plasmons in a rigorous and self-consistent way. For more detail on Maxwell-Bloch description, see Supporting Information S7.

In Figure 4a, we plot the near-field $E_z(x = 0)$ time evolution after a broadband pulsed excitation without ($E_{em}^{cav}$, red) and with ($E_{em}^{cav}$ blue) an emitter placed 0.5 nm from a nanoparticle of diameter 40 nm. The population of the excited state is also plotted on the same time-scale, which peaks at ~20 fs. A qualitatively similar behavior is observed for the NPoM (Figure 4b) but with 4x stronger field enhancement and 200x larger excited state population. To clearly demonstrate the induced E-field from the emitter $E_{em}^{cav} = E_{em}^{cav} - E_{em}^{cav}$, we separate the field due to emitter-plasmon coupling $E_{em}^{cav}$ from the field due to direct plasmon excitation $E_{em}^{cav}$. In Figure 4c,d, we plot $E_{em}^{cav}$ for emitters placed at various lateral positions away from closest proximity to both the isolated NP and the NPoM. For emitters at $x < 5$ nm from the isolated NP, $E_{em}^{cav}$ reduces, despite the stronger field enhancement. This shows that energy from the emitter is quenched due to coupling with nonradiative higher-order modes that are confined to the vicinity of the isolated NP. For the NPoM, as the emitter approaches the nanocavity $E_{em}^{cav}$ is instead increasingly enhanced.

Similar behavior is observed from the excited state population dynamics (Figure 4e,f). For $x < 2.5$ nm from the isolated NP, the population of the excited state is truncated by decay into the nonradiative channels, reducing it below that for an emitter at $x = 5$ nm, a behavior not present for the NPoM.

**Figure 4.** $E_z$ and excited state population $N_2$ dynamics for (a, c, e) isolated NP and (b, d, f) 1 nm wide NPoM of diameter 40 nm for a two-level emitter placed 0.5 nm below the nanoparticle. (a, b) $E_z$ (red, blue) and $N_2$ (black) dynamics for the structures without (red) and with (blue) the presence of the emitter at $x = 0$. (c, d) The corresponding induced $E$-fields from the emitter $E_{em}^{cav} = E_{em}^{cav} - E_{em}^{cav}$ and (e, f) the excited state population $N_2$ of the emitter, laterally displaced at $x = 0, 1.25, 2.5, 5$, and 10 nm. The emitters’ transition wavelengths are $\lambda_0 = 550$ and 700 nm, tuned to the dipole plasmonic mode of each system.
the two-level Maxwell-Bloch model; (8) lifetimes of an emitter placed in the nanocavities (PDF).

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**Notes**

The authors declare no competing financial interest.

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